

*Montana*  
*Comprehensive Assessment*  
*System (MontCAS, Phase 2)*  
*Criterion-Referenced Test (CRT)*

COMMON CONSTRUCTED-RESPONSE ITEM RELEASE  
MATHEMATICS, GRADE 8

2005



**OPI**

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# Mathematics

## Session 1 (Calculator)

**You may use a calculator during this session.**

25. The drama club put on a play on Friday night. They sold some tickets in advance and some tickets at the door. A total of 300 tickets were sold.

- a. Using  $x$  to represent the number of tickets sold in advance, write an expression that represents the number of tickets sold at the door.

The club charged \$3 for tickets sold in advance and \$4 for tickets sold at the door. The total amount of money collected from tickets was \$1072.

- b. Again using  $x$  to represent the number of tickets sold in advance, write one equation that can be used to find the number of \$3 tickets and the number of \$4 tickets sold. Your equation should contain no variables except  $x$ .
- c. How many \$3 tickets and how many \$4 tickets were sold? Show your work or explain how you found your answer.

## Scoring Guide

Score	Description
4	4 points
3	3 points
2	2 points
1	1 point OR Student shows minimal understanding of writing the expression or the equation or of solving the problem.
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.
Blank	No response.

### Training Notes:

Part a: 1 point for the correct answer,  $300 - x$

Part b: 1 point for the correct equation,  $1072 = 3x + 4(300 - x)$ , or equivalent, or for correct equation based on student's answer to Part a

Part c: 2 points for the correct answers, **128 \$3 tickets and 172 \$4 tickets**, or for correct answers based on student's equation in Part b, with work or explanation.

Note: Student does NOT have to use the algebraic solution.

OR

1 point for the correct answers without work or explanation.

or

for 1 correct answer with work shown.

or

for some correct strategy shown.

Score Point 4

Sample 1

$$a. \begin{array}{ccc} 300 & - & x & = & d \\ \text{total} & & \text{chance} & & \text{dase} \\ \text{tickets} & & \text{tickets} & & \text{tickets} \end{array}$$

$$b. \$3x + \$4(300-x) = \$1072$$

$$c. \$3x + \$4(300-x) = \$1072$$

$$3x + 1200 + 4x = 1072$$

$$-x + \overset{-1200}{1200} = \overset{-1200}{1072}$$

$$-x = -128$$

$$x = 128$$

128 tickets  
at \$3 were sold

172 tickets       $300 - 128 = 172$   
at \$4 were sold

Score Point 3

Sample 1

a. let  $y$  = tickets sold @ the door

$$300 - x = y$$

$$b. 3x + 4y = 1072$$

$$c. 3x + 4y = 1072$$

$$e. 300 - x = y$$

$$300 - x = y$$
$$\begin{array}{r} 300 - x = y \\ -300 \quad -300 \end{array}$$

$$-x = y - 300$$

$$x = -y + 300$$

$$3(-y + 300) + 4y = 1072$$

$$-3y + 900 + 4y = 1072$$

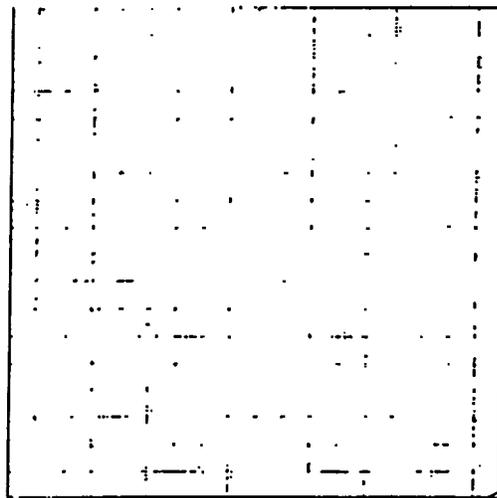
$$900 + y = 1072$$

$$y = 172$$

Note to self:  
= LABEL =

172 tickets were sold at the door and 128 tickets were sold in advance

If you substitute 128 for  $x$  and 172 for  $y$  you get 1072.



Score Point 2

Sample 1

a.  $300 - x =$  tickets sold at the door  
( $x =$  tickets sold in advance)

b.  $300 - x = \frac{(1072 - 3x)}{4} ?$

c. \$3 = 126

\$4 = 174

Score Point 1

Sample 1

$$a = 300 - x = n \text{ (tickets sold at the door)}$$

$$b = \$1072 \div 2 = n, (536)$$

$$c = \$1072 \div 2 = 536$$

$$536 \div 4 = 134 \text{ tickets}$$

$$536 \div 3 = 179 \text{ tickets}$$

Sample 2

$a. 300 = x + d$        $x = \text{tickets sold in advance}$   
 $b. \$1072 = 3x + 2d$        $d = \text{tickets sold at door}$

$c. \$1072 = 8d + 2d$        $1072 = 3d$   
 $996d = 1436$        $300 = x + d$   
 $574d = 1436$        $300 - d = x$   
 $200 \div 2 = 100$        $900 - 3d = 3x$   
 $100 - 8 = 450$        $1072 = (900 - 3d) + d$   
 $15d = 100$        $1072 = 900 - 2d$   
 $460 + 600 = 1060$        $1072 + 2d = 900$   
 $2d \div 3 = 7.3$        $2d = 172$   
 $2d \div 4 = 5.5$        $d = 86$   
 $155.5 \div 4 = 622$        $x = 271$   
 $111.5 \div 3 = 435.5$   
 $422 + 423.5 = 1055.5$   
 $16.5 \div 3 = 5.5$   
 $16.5 \div 4 = 4.125$   
 $155.5$

Score Point 0

Sample 1

I chose a number and multiplied it by 3 & 4. Then once I found one of the right numbers, I found the other. Next I added them together & got my answers.

$$\begin{array}{r} X = \text{tickets in advance} \quad \$3.00 \\ Y = \text{tickets at doors} \quad \$4.00 \\ \hline \$300 \end{array}$$

$$\begin{array}{l} \$4.00 \text{ tickets} = 42 \frac{1}{2} \text{ tickets} \\ \$3.00 \text{ tickets} = 43 \text{ tickets} \end{array}$$

# Mathematics

## Session 3 (No Calculator)

You may **NOT** use a calculator during this session.

68. Trisha surveyed 28 of her classmates by asking them to list the activities in which they participate in the summer. This table shows the results.

**Summer Activities**

Activity	Percent of Students
Read	75%
Play sports	21%
Visit friends	33%

- On the grid in your Student Response Booklet, make a bar graph of these data.
- Trisha wanted to make a circle graph to display her results. Explain why a circle graph would not be a good choice for these data.
- What is a question that Trisha could have asked about summer activities so that the results could be displayed in a circle graph?

## Scoring Guide

Score	Description
4	4 points
3	3 points
2	2 points
1	1 point
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.
<b>Blank</b>	No response.

### Training Notes:

Part a. 2 points for a correct bar graph, with axes correctly labeled, scale correct, and data correctly represented.

OR

1 point for a bar graph that is mostly correct. Some labels may be missing or there may be interval errors.

Part b. 1 point for an explanation why a circle graph is not good for these data.

For example, "To use a circle graph the sum of the percents must be 100%."

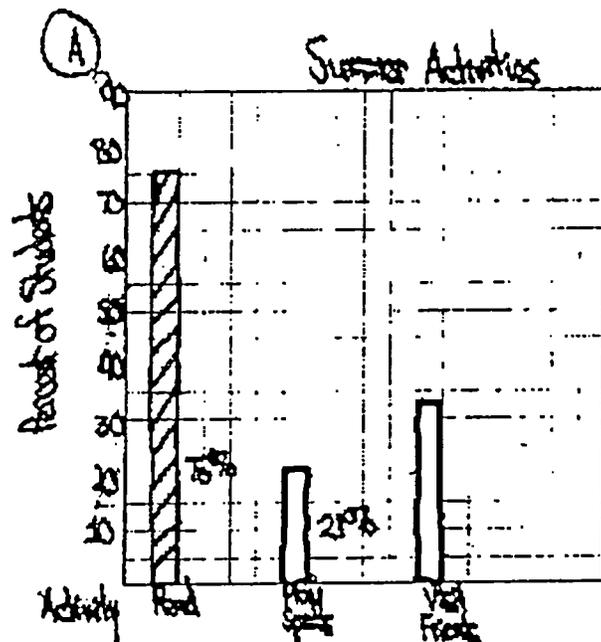
Part c. 1 point for a question that will give results that total 100%.

For example, "What is your favorite summer activity?"

Score Point 4

Sample 1

- (B) She shouldn't use a circle graph because the percents don't equal up to 100% so she wouldn't know how big to make each section.
- (C) What is your favorite summer activity? This question would make the percents equal up to 100%.



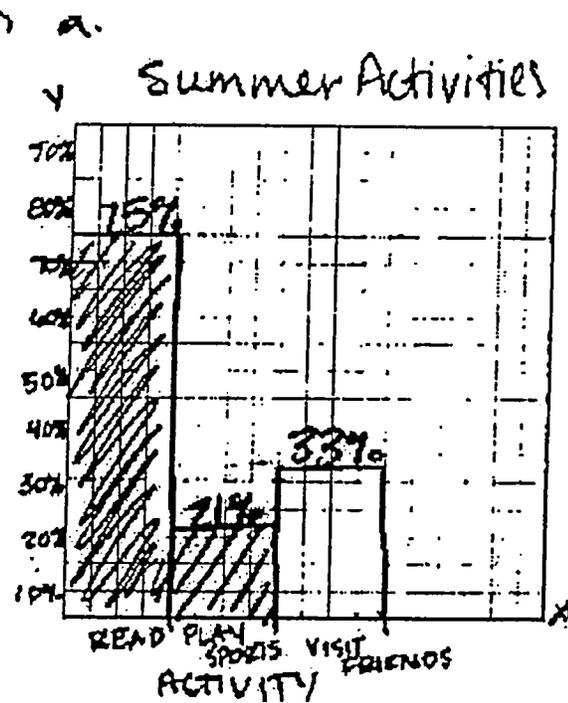
Score Point 3

Sample 1

b. A circle graph wouldn't be good b/c girls can do more than one summer activity, so your results wouldn't add up to exactly 100%.

c. What is your one most favorite activity to do in the summer?

% of girls doing the activity



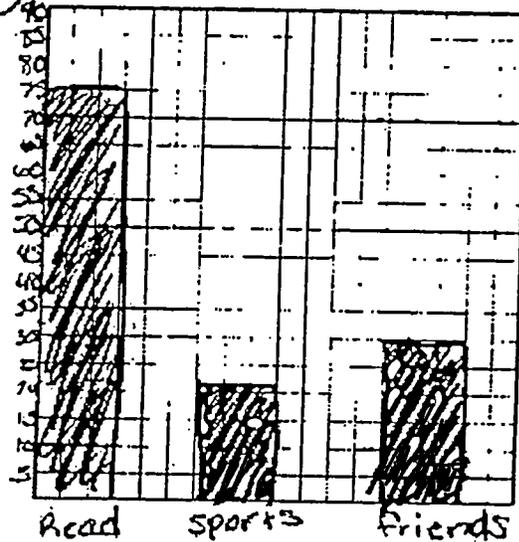
Score Point 2

Sample 1

(b) A circle graph would not work because not all the information would fit.

(c) What was your main activity this summer?

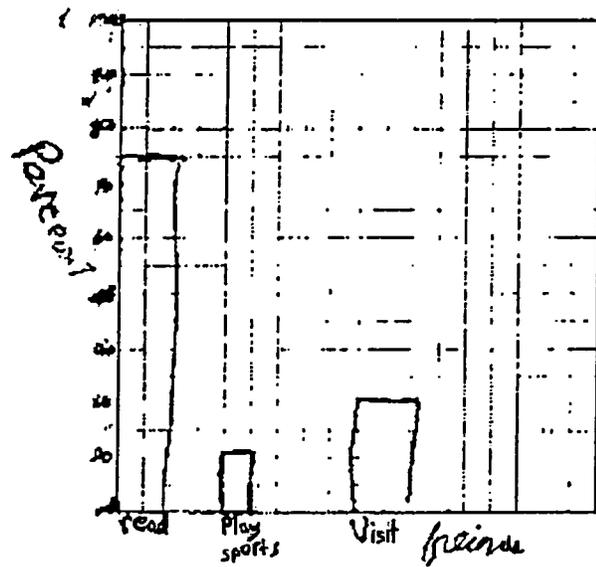
(A)



Score Point 1

Sample 1

A  
B.E. could be.  
C.E. could be.



Score Point 0

Sample 1

- a. See graph b. Because There aren't enough categories to make a circle graph.
- c. Did anyone do arts and crafts, Or go and visit other relatives. Did anyone go to the water slides? Did anyone go camping?

